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tsxtreme-package

Bayesian Modelling of Extremal Dependence in Time Series

Description

Characterisation of the extremal dependence structure of time series, avoiding pre-processing and filtering as done typically with peaks-over-threshold methods. It uses the conditional approach of Heffernan and Tawn (2004) <DOI:10.1111/j.1467-9868.2004.02050.x> which is very flexible in terms of extremal and asymptotic dependence structures, and Bayesian methods improve efficiency and allow for deriving measures of uncertainty. For example, the extremal index, related to the size of clusters in time, can be estimated and samples from its posterior distribution obtained.

Details

Index: This package was not yet installed at build time.

The Heffernan–Tawn conditional formulation for a stationary time series (X_t) with Laplace marginal distribution states that for a large enough threshold u there exist scale parameters $-1 \le \alpha_j \le 1$ and $0 \le \beta_j \le 1$ such that

$$Pr\left(\frac{X_j - \alpha_j X_0}{(X_j)^{\beta_j}} < z_j, j = 1, \dots, m \mid X_0 > u\right) = H(z_1, \dots, z_m),$$

with H non-degenerate; the equality holds exactly only when u tends to infinity.

There are mainly 3 functions provided by this package, which allow estimation of extremal dependence measures and fitting the Heffernan–Tawn model using Dirichlet processes.

depfit fits the Heffernan-Tawn model using a Bayesian semi-parametric approach.

thetafit computes posterior samples of the threshold-based index of Ledford and Tawn (2003) based on inference in depfit.

chifit computes posterior samples of the extremal measure of dependence of Coles, Heffernan and Tawn (1999) at any extremal level.

Some corresponding functions using the stepwise approach of Heffernan and Tawn (2004) are also part of the package, namely dep2fit and theta2fit.

The empirical estimation of the extremal index can be done using thetaruns and some basic functions handling the Laplace distribution are also available in dlapl.

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References

Coles, S., Heffernan, J. E. and Tawn, J. A. (1999) Dependence measures for extreme value analyses. *Extremes*, **2**, 339–365.

Davison, A. C. and Smith, R. L. (1990) Models for exceedances over high thresholds. *Journal of the Royal Statistical Society Series B*, **52**, 393–442.

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Ledford, W. A. and Tawn, J. A. (2003) Diagnostics for dependence within time series extremes. *Journal of the Royal Statistical Society Series B*, **65**, 521–543.

Lugrin, T., Davison, A. C. and Tawn, J. A. (2016) Bayesian uncertainty management in temporal dependence of extremes. *Extremes*, **19**, 491–515.

See Also

thetafit, chifit, depfit

bayesfit

Traces from MCMC output

Description

Test or show objects of class "bayesfit".

Usage

is.bayesfit(x)

Arguments

х

an arbitrary R object.

Details

Default plot shows samples of residual densities (which==1), residual distribution with credible interval (5% and 95% posterior quantiles; which==2), and joint posterior distribution of α and β (which==3) for each lag successively. which can be any composition of 1,2 and 3.

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Value

An object of class "bayesfit" is a list containing MCMC traces for:

a, b Heffernan-Tawn parameters.

sd, mean, w standard deviations, means and weights of the mixture components.

prec precision parameter of the Dirichlet process.

ci auxiliary variable; components' indices for each observation.

noo number of observations in each mixture component.
noc number of non-empty components in the mixture.

prop. sd standard deviations of the proposal distributions for a and b.

And len, the length of the traces, i.e., the number of iterations saved.

See Also

bayesparams, stepfit

bayesparams

Parameters for the semi-parametric approach

Description

Create, test or show objects of class "bayesparams".

Usage

```
bayesparams(prop.a = 0.02, prop.b = 0.02,
    prior.mu = c(0, 10), prior.nu = c(2, 1/2), prior.eta = c(2, 2),
    trunc = 100, comp.saved = 15, maxit = 30000,
    burn = 5000, thin = 1,
    adapt = 5000, batch.size = 125,
    mode = 1)

is.bayesparams(x)
```

prop.a, prop.b	standard deviation for the Gaussian proposal of the Heffernan–Tawn parameters.
prior.mu	mean and standard deviation of the Gaussian prior for the components' means.
prior.nu	shape and rate of the inverse gamma prior for the components' variances.
prior.eta	shape and scale of the gamma prior for the precision parameter of the Dirichlet process.
trunc	integer; value of the truncation for the approximation of the infinite sum in the stick-breaking representation.

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comp.saved	number of first components to be saved and returned.
maxit	maximum number of iterations.
burn	number of first iterations to discard.
thin	positive integer; spacing between iterations to be saved. Default is 1, i.e., all iterations are saved.
adapt	integer; number of iterations during which an adaption algorithm is applied to the proposal variances of α and β .
batch.size	size of batches used in the adaption algorithm. It has no effect if adapt==0.
mode	verbosity; 0 for debug mode, 1 (default) for standard output, and 2 for silent.
X	an arbitrary R object.

Details

prop. a is a vector of length 5 with the standard deviations for each region of the RAMA for the (Gaussian) proposal for α . If a scalar is given, 5 identical values are assumed.

prop.b is a vector of length 3 with the standard deviations for each region of the RAMA for the (Gaussian) proposal for β . If a scalar is provided, 3 identical values are assumed.

comp. saved has no impact on the calculations: its only purpose is to prevent from storing huge amounts of empty components.

The regional adaption scheme targets a 0.44 acceptance probability. It splits [-1;1] in 5 regions for α and [0;1] in 3 regions for β . The decision to increase/decrease the proposal standard deviation is based on the past batch. size MCMC iterations, so too low values yield inefficient adaption, while too large values yield slow adaption.

Default values for the hyperparameters are chosen to get reasonably uninformative priors.

See Also

```
bayesfit, depmeasure
```

Examples

```
is.bayesparams(bayesparams()) # TRUE
## use defaults, change max number of iteration of MCMC
par <- bayesparams(maxit=1e5)</pre>
```

|--|

Description

The conditional Heffernan–Tawn model is used to fit the dependence in time of a stationary series. A standard 2-stage procedure is used.

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Usage

Arguments

ts	numeric vector; time series to be fitted.
u.mar	marginal threshold; used when transforming the time series to Laplace scale.
u.dep	dependence threshold; level above which the dependence is modelled. $u.dep$ can be lower than $u.mar$.
lapl	logical; is ts on the Laplace scale already? The default (FALSE) assumes unknown marginal distribution.
method.mar	a character string defining the method used to estimate the marginal GPD; either "mle" for maximum likelihood of "mom" for method of moments. Defaults to "mle".
nlag	integer; number of lags to be considered when modelling the dependence in time.
conditions	logical; should conditions on α and β be set? (see Details) Defaults to TRUE.

Details

Consider a stationary time series (X_t) with Laplace marginal distribution; the fitting procedure consists of fitting

$$X_t = \alpha_t \times x_0 + x_0^{\beta_t} \times Z_t, \quad t = 1, \dots, m,$$

with m the number of lags considered. A likelihood is maximised assuming $Z_t \sim N(\mu_t, \sigma_t^2)$, then an empirical distribution for the Z_t is derived using the estimates of α_t and β_t and the relation

$$\hat{Z}_t = \frac{X_t - \hat{\alpha}_t \times x_0}{x_0^{\hat{\beta}_t}}.$$

conditions implements additional conditions suggested by Keef, Papastathopoulos and Tawn (2013) on the ordering of conditional quantiles. These conditions help with getting a consistent fit by shrinking the domain in which (α, β) live.

Value

alpha	parameter controlling the conditional extremal expectation.
beta	parameter controlling the conditional extremal expectation and variance.
res	empirical residual of the model.
pars.se	vector of length 2 giving the estimated standard errors for alpha and beta given by the hessian matrix of the likelihood function used in the first step of the inference procedure.

See Also

depfit, theta2fit

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Examples

```
## generate data from an AR(1)
## with Gaussian marginal distribution
n <- 10000
dep <- 0.5
ar <- numeric(n)</pre>
ar[1] <- rnorm(1)
for(i in 2:n)
  ar[i] <- rnorm(1, mean=dep*ar[i-1], sd=1-dep^2)</pre>
plot(ar, type="l")
plot(density(ar))
grid <- seq(-3,3,0.01)
lines(grid, dnorm(grid), col="blue")
## rescale margin
ar <- qlapl(pnorm(ar))</pre>
## fit model without constraints...
fit1 <- dep2fit(ts=ar, u.mar = 0.95, u.dep=0.98, conditions=FALSE)</pre>
fit1$a; fit1$b
## ...and compare with a fit with constraints
fit2 <- dep2fit(ts=ar, u.mar = 0.95, u.dep=0.98, conditions=TRUE)
fit2$a; fit2$b# should be similar, as true parameters lie well within the constraints
```

depfit

Dependence model fit

Description

Bayesian semiparametrics are used to fit the Heffernan–Tawn model to time series. Options are available to impose a structure in time on the model.

Usage

```
depfit(ts, u.mar = 0, u.dep=u.mar,
    lapl = FALSE, method.mar=c("mle","mom","pwm"),    nlag = 1,
    par = bayesparams(),
    submodel = c("fom", "none", "ugm"))
```

ts	numeric vector; time series to be fitted.
u.mar	marginal threshold; used when transforming the time series to Laplace scale.
u.dep	dependence threshold; level above which the dependence is modelled. $u.dep$ can be lower than $u.mar$.
lapl	logical; is ts on the Laplace scale already? The default (FALSE) assumes unknown marginal distribution.

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method.mar a character string defining the method used to estimate the marginal GPD; either

"mle" for maximum likelihood or "mom" for method of moments or "pwm" for

probability weighted moments. Defaults to "mle".

nlag integer; number of lags to be considered when modelling the dependence in

time.

par an object of class 'bayesparams'.

submodel a character string; "fom" for first order Markov, "none" for no particular time

structure, or "ugm" for univariate Gaussian mixture (see details).

Details

submodel can be "fom" to impose a first order Markov structure on the model parameters α_j and β_j (see thetafit for more details); it can take the value "none" to impose no particular structure in time; it can also be "ugm" which can be applied to density estimation, as it corresponds to setting $\alpha = \beta = 0$ (see examples).

Value

An object of class 'bayesfit' with elements:

a posterior trace of α . b posterior trace of β .

sd posterior trace of the components' standard deviations.

mean posterior trace of the components' means.

w posterior trace of the components' assigned weights.

prec posterior trace of the precision parameter.

noo posterior trace of the number of observations per component.

prop.sd posterior trace of the number of components containing at least one observation. prop.sd trace of proposal standard deviations in the 5+3 regions of the adaption scheme

for α and β .

len length of the returned traces.

See Also

```
thetafit, chifit
```

```
## generate data from an AR(1)
## with Gaussian marginal distribution
n <- 10000
dep <- 0.5
ar <- numeric(n)
ar[1] <- rnorm(1)
for(i in 2:n)
    ar[i] <- rnorm(1, mean=dep*ar[i-1], sd=1-dep^2)</pre>
```

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```
## rescale the margin
ar <- qlapl(pnorm(ar))

## fit the data
params <- bayesparams()
params$maxit <- 100# bigger numbers would be
params$burn <- 10 # more sensible...
params$thin <- 4
fit <- depfit(ts=ar, u.mar=0.95, u.dep=0.98, par=params)

########

## density estimation with submodel=="ugm"
data <- MASS::galaxies/1e3
dens <- depfit(ts=data, par=params, submodel="ugm")</pre>
```

depmeasure

Dependence measures estimates

Description

Test or show objects of class "depmeasure".

Usage

```
is.depmeasure(x)
```

Arguments

x an arbitrary R object.

Value

An object of class 'depmeasure' is a list which contains:

fit an object of class 'bayesfit'

distr an array with the samples used for the estimation.

probs, levels points —probability and original scale respectively— at which the dependence

measure is estimated

Depending on the dependence measure, theta or chi, a matrix with levels on row-entries and mean, median and specified quantiles of the posterior distribution of theta or chi respectively.

See Also

depmeasures

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depmeasures

Estimate dependence measures

Description

Appropriate marginal transforms are done before the fit using standard procedures, before the dependence model is fitted to the data. Then the posterior distribution of a measure of dependence is derived. thetafit gives posterior samples for the extremal index $\theta(x,m)$ and chifit does the same for the coefficient of extremal dependence $\chi_m(x)$.

Usage

```
thetafit(ts, lapl = FALSE, nlag = 1,
      R = 1000, S = 500,
      u.mar = 0, u.dep,
      probs = seq(u.dep, 0.9999, length.out = 30),
      method.mar = c("mle", "mom", "pwm"), method = c("prop", "MCi"),
      silent = FALSE,
      fit = TRUE, prev.fit=bayesfit(), par = bayesparams(),
      submodel = c("fom", "none"), levels=c(.025, .975))
chifit(ts, lapl = FALSE, nlag = 1,
      R = 1000, S = 500,
      u.mar = 0, u.dep,
      probs = seq(u.dep, 0.9999, length.out = 30),
      method.mar = c("mle", "mom", "pwm"), method = c("prop", "MCi"),
      silent = FALSE,
      fit = TRUE, prev.fit=bayesfit(), par = bayesparams(),
      submodel = c("fom", "none"), levels=c(.025, .975))
```

ts	a vector, the time series for which to estimate the extremal index $\theta(x,m)$ or the coefficient of extremal dependence $\chi_m(x)$, with x a probability level and m a run-length (see details).
lapl	logical; TRUE indicates that ts has a marginal Laplace distribution. If FALSE (default), method.mar is used to transform the marginal distribution of ts to Laplace.
nlag	the run-length; an integer larger or equal to 1.
R	the number of samples per MCMC iteration drawn from the sampled posterior distributions; used for the estimation of the dependence measure.
S	the number of posterior distributions sampled to be used for the estimation of the dependence measure.
u.mar	probability; threshold used for marginal transformation if lapl is FALSE. Not used otherwise.

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u.dep	probability; threshold used for the extremal dependence model.
probs	vector of probabilities; the values of x for which to evaluate $\theta(x, m)$ or $\chi_m(x)$.
method.mar	a character string defining the method used to estimate the marginal GPD; either "mle" for maximum likelihood of "mom" for method of moments or "pwm" for probability weighted moments methods. Defaults to "mle".
method	a character string defining the method used to estimate the dependence measure; either "prop" for proportions or "MCi" for Monte Carlo integration (see details).
silent	logical (FALSE); verbosity.
fit	logical; TRUE means that the dependence model must be fitted and the values in par are used. Otherwise the result from a previous call to depfit.
prev.fit	an object of class 'bayesfit'. Needed if fit is FALSE. Typically returned by a previous call to depfit.
par	an object of class 'bayesparams' to be used for the fit of dependence model.
submodel	a character string, either "fom" for first order Markov or "none" for no specification.
levels	vector of probabilites; the quantiles of the posterior distribution of the extremal measure to be computed.

Details

The sub-asymptotic extremal index is defined as

$$\theta(x, m) = Pr(X_1 < x, \dots, X_m < x | X_0 > x),$$

whose limit as x and m go to ∞ appropriately is the extremal index θ . The extremal index can be interpreted as the inverse of the asymptotic mean cluster size (see thetaruns).

The sub-asymptotic coefficient of extremal dependence is

$$\chi_m(x) = Pr(X_m > x | X_0 > x),$$

whose limit χ defines asymptotic dependence ($\chi > 0$) or asymptotic independence ($\chi = 0$).

Both types of extremal dependence measures can be estimated either using a

- * proportion method (method == "prop"), sampling from the conditional probability given $X_0 > x$ and counting the proportion of sampled points falling in the region of interest, or
- * Monte Carlo integration (method == "MCi"), sampling replicates from the marginal exponential tail distribution and evaluating the conditional tail distribution in these replicates, then taking their mean as an approximation of the integral.

submodel == "fom" imposes a first order Markov structure to the model, namely a geometrical decrease in α and a constant β across lags, i.e. $\alpha_j = \alpha^j$ and $\beta_j = \beta, j = 1, \dots, m$.

Value

An object of class 'depmeasure', containing a subset of:

bayesfit An object of class 'bayesfit'

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An array with dimensions m × length(probs) × (2+length(levels)), with the last dimension listing the posterior mean and median, and the level posterior quantiles

distr

An array with dimensions m × length(probs) × S; posterior samples of theta

chi

An array with dimensions m × length(probs) × (2+length(levels)), with the last dimension listing the posterior mean and median, and the level posterior quantiles

probs

probs

probs

probs transformed to original scale of ts

See Also

```
depfit, theta2fit, thetaruns
```

```
## generate data from an AR(1)
## with Gaussian marginal distribution
   <- 10000
dep <- 0.5
      <- numeric(n)
ar[1] <- rnorm(1)
for(i in 2:n)
  ar[i] \leftarrow rnorm(1, mean=dep*ar[i-1], sd=1-dep^2)
plot(ar, type="l")
plot(density(ar))
grid <- seq(-3,3,0.01)
lines(grid, dnorm(grid), col="blue")
## rescale the margin (focus on dependence)
ar <- qlapl(pnorm(ar))</pre>
## fit the data
params <- bayesparams()</pre>
params$maxit <- 100 # bigger numbers would be
params$burn <- 10 # more sensible...
params$thin <- 4
theta <- thetafit(ts=ar, R=500, S=100, u.mar=0.95, u.dep=0.98,
                  probs = c(0.98, 0.999), par=params)
## or, same thing in two steps to control fit output before computing theta:
fit <- depfit(ts=ar, u.mar=0.95, u.dep=0.98, par=params)</pre>
plot(fit)
theta <- thetafit(ts=ar, R=500, S=100, u.mar=0.95, u.dep=0.98,
                  probs = c(0.98, 0.999), fit=FALSE, prev.fit=fit)
```

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Laplace	The Laplace Distribution

Description

Density, distribution function, quantile function and random generation for the Laplace distribution with location parameter loc and scale parameter scale.

Usage

```
dlapl(x, loc = 0, scale = 1, log = FALSE)
plapl(q, loc = 0, scale = 1, lower.tail = TRUE, log.p = FALSE)
qlapl(p, loc = 0, scale = 1, lower.tail = TRUE, log.p = FALSE)
rlapl(n, loc = 0, scale = 1)
```

Arguments

x, q	vector of quantiles.
р	vector of probabilities.
n	number of samples to generate.
loc	vector of location parameters.
scale	vector of scale parameters. These must be positive.
lower.tail	logical; if TRUE (default), probabilities are $Pr(X \leq x)$, otherwise $Pr(X > x)$.
log, log.p	logical; if TRUE, probabilities p are given as $log(p)$.

Details

If loc or scale are not specified, they assume the default values of 0 and 1 respectively.

The Laplace distribution has density

$$f(x) = \exp(-|x - \mu|/\sigma)/(2\sigma)$$

where μ is the location parameter and σ is the scale parameter.

Value

dlapl gives the density, plapl gives the distribution function, qlapl gives the quantile function, and rlapl generates random deviates.

The length of the result is determined by n in rlapl, and is the maximum of the lengths of the numerical arguments for the other functions. Standard R vector operations are to be assumed.

If sd=0, the limit as sd decreases to 0 is returned, i.e., a point mass at loc. The case sd<0 is an error and nothing is returned.

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Warning

Some checks are done previous to standard evaluation, but vector computations have not yet been tested thoroughly! Typically vectors not having lengths multiple of each other return an error.

See Also

dexp for the exponential distribution which is the positive part of the Laplace distribution.

Examples

```
## evaluate the density function on a grid of values
x <- seq(from=-5, to=5, by=0.1)
fx <- dlapl(x, loc=1, scale=.5)

## generate random samples of a mixture of Laplace distributions
rnd <- rlapl(1000, loc=c(-5,-3,2), scale=0.5)

## an alternative:
rnd <- runif(1000)
rnd <- qlapl(rnd, loc=c(-5,-3,2), scale=0.5)

## integrate the Laplace density on [a,b]
a <- -1
b <- 7
integral <- plapl(b)-plapl(a)</pre>
```

stepfit

Estimates from stepwise fit

Description

Create, test or show objects of class "stepfit".

Usage

```
stepfit()
is.stepfit(x)
```

Arguments

Χ

an arbitrary R object.

Value

An object of class "stepfit" is a list containing:

a, b Heffernan–Tawn parameters.

res fitted residuals.

pars.se estimated standard error of a and b.

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See Also

bayesfit, depmeasure

theta2fit Fit time series extremes	fit Fit time series extremes	
------------------------------------	------------------------------	--

Description

Appropriate marginal transforms are done before the fit using standard procedures, before the dependence model is fitted to the data. Then the measure of dependence $\theta(x,m)$ is derived using a method described in Eastoe and Tawn (2012).

Usage

ts	numeric vector; time series to be fitted.
lapl	logical; is to on the Laplace scale already? The default (FALSE) assumes unknown marginal distribution.
nlag	integer; number of lags to be considered when modelling the dependence in time.
R	integer; the number of samples used for estimating $\theta(x, m)$.
u.mar	marginal threshold; used when transforming the time series to Laplace scale if lapl is FALSE; not used otherwise.
u.dep	dependence threshold; level above which the dependence is modelled. $u.dep$ can be lower than $u.mar$.
probs	vector of probabilities; the values of x for which to evaluate $\theta(x, m)$.
method.mar	a character string defining the method used to estimate the marginal GPD; either "mle" for maximum likelihood of "mom" for method of moments or "pwm" for probability weighted moments methods. Defaults to "mle".
method	a character string defining the method used to estimate the dependence measure; either "prop" for proportions or "MCi" for Monte Carlo integration (see Details).
silent	logical (FALSE); verbosity.
R.boot	integer; the number of samples used for the block bootstrap for the confidence intervals.
block.length	integer; the block length used for the block-bootstrapped confidence intervals.
levels	vector of probabilities; the quantiles of the bootstrap distribution of the extremal measure to be computed.

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Details

The standard procedure (method="prop") to estimating probabilities from a Heffernan-Tawn fit best illustrated in the bivariate context $(Y \mid X > u)$:

- 1. sample X from an exponential distribution above $v \geq u$,
- 2. sample Z (residuals) from their empirical distribution,
- 3. compute Y using the relation $Y = \alpha \times X + X^{\beta} \times Z$,
- 4. estimate $Pr(X > v_x, Y > v_y)$ by calculating the proportion p of Y samples above v_y and multiply p with the marginal survival distribution evaluated at v_x .

With method="MCi" a Monte Carlo integration approach is used, where the survivor distribution of Z is evaluated at pseudo-residuals of the form

$$\frac{v_y - \alpha \times X}{X^{\beta}},$$

where X is sampled from an exponential distribution above v_x . Taking the mean of these survival probabilities, we get the Monte Carlo equivalent of p in the proportion approach.

Value

List containing:

depfit an object of class 'stepfit'

probs probs

levels probs transformed to original scale of ts

theta a matrix with proportion or Monte Carlo estimates of $\theta(x, m)$. Rows correspond

to values in probs, columns are point estimates and bootstrap quantiles

See Also

```
dep2fit, thetafit, thetaruns
```

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```
## fit the data
fit <- theta2fit(ts=ar, u.mar=0.95, u.dep=0.98)
## plot theta(x,1)
plot(fit)
abline(h=1, lty="dotted")</pre>
```

thetaruns

Runs estimator

Description

Compute the empirical estimator of the extremal index using the runs method (Smith & Weissman, 1994, JRSSB).

Usage

ts	a vector, the time series for which to estimate the threshold-based extremal index $\theta(x,m)$, with x a probability level and m a run-length (see details).
lapl	logical; is ts on the Laplace scale already? The default (FALSE) assumes unknown marginal distribution.
nlag	the run-length; an integer larger or equal to 1.
u.mar	marginal threshold (probability); used when transforming the time series to Laplace scale if lapl is FALSE; if lapl is TRUE, it is nevertheless used when bootstrapping, since the bootstrapped series generally do not have Laplace marginal distributions.
probs	vector of probabilities; the values of x for which to evaluate $\theta(x, m)$.
method.mar	a character string defining the method used to estimate the marginal GPD; either "mle" for maximum likelihood or "mom" for method of moments or "pwm" for probability weighted moments methods. Defaults to "mle".
block.length	integer; the block length used for the block-bootstrapped confidence intervals.
R.boot	integer; the number of samples used for the block bootstrap.
levels	vector of probabilites; the quantiles of the posterior distribution of the extremal index $\theta(x,m)$ to output.

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Details

Consider a stationary time series (X_t) . A characterisation of the extremal index is

$$\theta(x,m) = Pr(X_1 \le x, \dots, X_m \le x \mid X_0 \ge x).$$

In the limit when x and m tend to ∞ appropriately, θ corresponds to the asymptotic inverse mean cluster size. It also links the generalised extreme value distribution of the independent series (Y_t) , with the same marginal distribution as (X_t) ,

$$G_Y(z) = G_X^{\theta}(z),$$

with G_X and G_Y the extreme value distributions of (X_t) and (Y_t) respectively.

nlag corresponds to the *run-length* m and probs is a set of values for x. The *runs* estimator is computed, which consists of counting the proportion of clusters to the number of exceedances of a threshold x; two exceedances of the threshold belong to different clusters if there are at least m+1 non-exceedances inbetween.

Value

An object of class 'depmeasure' containing:

theta matrix; estimates of the extremal index $\theta(x,m)$ with rows corresponding to the

probs values of x and the columns to the runs estimate and the chosen levels-

quantiles of the bootstrap distribution.

nbr.exc numeric vector; number of exceedances for each threshold corresponding to the

elements in probs.

probs probs.

levels numeric vector; probs converted to the original scale of ts.

nlag nlag.

See Also

```
theta2fit, thetafit
```

```
## generate data from an AR(1)
## with Gaussian marginal distribution
n <- 10000
dep <- 0.5
ar <- numeric(n)
ar[1] <- rnorm(1)
for(i in 2:n)
    ar[i] <- rnorm(1, mean=dep*ar[i-1], sd=1-dep^2)
## transform to Laplace scale
ar <- qlapl(pnorm(ar))
## compute empirical estimate
theta <- thetaruns(ts=ar, u.mar=.95, probs=c(.95,.98,.99))
## output
plot(theta, ylim=c(.2,1))
abline(h=1, lty="dotted")</pre>
```

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